| 1(a)(i) | $\begin{aligned} & {[\text { Velocity }]=\mathrm{LT}^{-1}} \\ & {[\text { Acceleration }]=\mathrm{LT}^{-2}} \\ & {[\text { Force }]=\mathrm{MLT}^{-2}} \\ & {[\text { Density }]=\mathrm{ML}^{-3}} \\ & {[\text { Pressure }]=\mathrm{ML}^{-1} \mathrm{~T}^{-2}} \end{aligned}$ | B1 <br> B1 <br> B1 <br> B1 <br> B1 <br> 5 | (Deduct 1 mark if answers given as $\mathrm{ms}^{-1}, \mathrm{~ms}^{-2}, \mathrm{kgms}^{-2}$ etc) |
| :---: | :---: | :---: | :---: |
| (ii) | $\left[\begin{array}{rl} {[P]=M L^{-1} \mathrm{~T}^{-2}} \\ {\left[\frac{1}{2} \rho v^{2}\right]} & =\left(\mathrm{ML}^{-3}\right)\left(\mathrm{LT}^{-1}\right)^{2} \\ & =\mathrm{ML}^{-1} \mathrm{~T}^{-2} \\ {[\rho g h]} & \left(\mathrm{ML}^{-3}\right)\left(\mathrm{LT}^{-2}\right)(\mathrm{L})=\mathrm{ML}^{-1} \mathrm{~T}^{-2} \end{array}\right.$ <br> All 3 terms have the same dimensions | $\left\|\begin{array}{ll} \text { M1 } & \\ \text { A1 } & \\ \text { A1 } & \\ \text { E1 } & \\ 4 \end{array}\right\|$ | Finding dimensions of 2nd or 3rd term <br> Allow e.g. ‘Equation is dimensionally consistent' following correct work |
| (b)(i) |  | M1 <br> A1 <br> 2 | For a 'cos' curve (starting at the highest point) <br> Approx correct values marked on both axes |
| (ii) | $\begin{gathered} \text { Period } \frac{2 \pi}{\omega}=3.49 \\ \omega=1.8 \\ h=1.9+0.3 \cos 1.8 t \end{gathered}$ | $\left\|\begin{array}{ll} \text { M1 } & \\ \text { A1 } & \\ \text { M1 } & \\ \text { F1 } & \\ \hline \end{array}\right\|$ | Accept $\frac{2 \pi}{3.49}$ <br> For $h=c+a \cos / \sin$ with either $c=\frac{1}{2}(1.6+2.2)$ or $a=\frac{1}{2}(2.2-1.6)$ |
| (iii) | When $h=1.7$, float is 0.2 m below centre Acceleration is $\omega^{2} x=1.8^{2} \times 0.2$ <br> $=0.648 \mathrm{~m} \mathrm{~s}^{-2}$ upwards | M1A1 <br> A1 cao | Award M1 if there is at most one error |
|  | $\begin{aligned} \text { OR When } h=1.7, \cos 1.8 t=-\frac{2}{3} & \\ & (1.8 t=2.30, t=1.28) \\ \text { Acceleration } \ddot{h}= & -0.3 \times 1.8^{2} \cos 1.8 t \quad \text { M1 } \\ = & -0.3 \times 1.8^{2} \times\left(-\frac{2}{3}\right) \\ & =0.648 \mathrm{~ms}^{-2} \text { upwards A1 cao } \end{aligned}$ |  |  |


| 2 (i) | $R \cos 60=0.4 \times 9.8$ <br> Normal reaction is 7.84 N | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ $2$ | Resolving vertically (e.g. $R \sin 60=m g$ is M1A0 $R=m g \cos 60$ is M0) |
| :---: | :---: | :---: | :---: |
| (ii) | $\begin{aligned} & R \sin 60=0.4 \times \frac{v^{2}}{2.7 \sin 60} \\ & \text { Speed is } 6.3 \mathrm{~ms}^{-1} \end{aligned}$ | M1 <br> M1 <br> A1 <br> A1 cao <br> 4 | Horizontal equation of motion Acceleration $\frac{v^{2}}{r}$ (M0 for $\frac{v^{2}}{2.7}$ ) |
|  | $\text { OR } \begin{gathered} \text { ORin } 60=0.4 \times(2.7 \sin 60) \omega^{2} \\ \omega=2.694 \\ v=(2.7 \sin 60) \omega \\ \\ \text { Speed is } 6.3 \mathrm{~ms}^{-1} \end{gathered}$ |  | Horizontal equation of motion or $R=0.4 \times 2.7 \times \omega^{2}$ <br> For $v=r \omega \quad(\mathrm{M} 0$ for $v=2.7 \omega)$ |
| (iii) | By conservation of energy, $\begin{aligned} \frac{1}{2} \times 0.4 \times\left(9^{2}-v^{2}\right) & =0.4 \times 9.8 \times(2.7+2.7 \cos \theta) \\ 81-v^{2} & =52.92+52.92 \cos \theta \\ v^{2} & =28.08-52.92 \cos \theta \end{aligned}$ | M1 <br> A1 <br> A1 <br> 3 | Equation involving KE and PE <br> Any (reasonable) correct form e.g. $v^{2}=81-52.92(1+\cos \theta)$ |
| (iv) | $\begin{aligned} R+0.4 \times 9.8 \cos \theta & =0.4 \times \frac{v^{2}}{2.7} \\ R+3.92 \cos \theta & =\frac{0.4}{2.7}(28.08-52.92 \cos \theta) \\ R+3.92 \cos \theta & =4.16-7.84 \cos \theta \\ R & =4.16-11.76 \cos \theta \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { E1 } \end{aligned}$ | Radial equation with 3 terms <br> Substituting expression for $v^{2}$ <br> $S R$ If $\theta$ is taken to the downward vertical, maximum marks are: <br> M1A0A0 in (iii) <br> M1A1M1A1E0 in (iv) |
| (v) | Leaves surface when $R=0$ $\begin{aligned} & \cos \theta=\frac{4.16}{11.76} \\ & v^{2}=28.08-52.92 \times \frac{4.16}{11.76} \quad(=9.36) \end{aligned}$ <br> Speed is $3.06 \mathrm{~m} \mathrm{~s}^{-1}$ | M1  <br> A1  <br> M1  <br>   <br> A1 cao  <br>  4 | Dependent on previous M1 or using $m g \cos \theta=\frac{m v^{2}}{r}$ |


| 3 (i) | Tension is $637 \times 0.1=63.7 \mathrm{~N}$ <br> Energy is $\frac{1}{2} \times 637 \times 0.1^{2}$ <br> $=3.185 \mathrm{~J}$ | $\left.\begin{array}{ll} \hline \text { B1 } & \\ \text { M1 } & \\ \text { A1 } & \\ & 3 \end{array} \right\rvert\,$ |  |
| :---: | :---: | :---: | :---: |
| (ii) | Let $\theta$ be angle between RA and vertical $\begin{gathered} \cos \theta=\frac{5}{13} \quad\left(\theta=67.4^{\circ}\right) \\ T \cos \theta=m g \\ 63.7 \times \frac{5}{13}=m \times 9.8 \end{gathered}$ <br> Mass of ring is 2.5 kg | $\begin{aligned} & \mathrm{B} 1 \\ & \mathrm{M} 1 \\ & \mathrm{~A} 1 \\ & \mathrm{E} 1 \end{aligned}$ $4$ | Resolving vertically |
| (iii) | Loss of PE is $2.5 \times 9.8 \times(0.9-0.5)$ <br> EE at lowest point is $\frac{1}{2} \times 637 \times 0.3^{2} \quad(=28.665)$ <br> By conservation of energy, $\begin{aligned} 2.5 \times 9.8 \times 0.4+\frac{1}{2} \times 2.5 u^{2} & =\frac{1}{2} \times 637 \times 0.3^{2}-3.185 \\ 9.8+1.25 u^{2} & =25.48 \\ u^{2} & =12.544 \\ u & =3.54 \end{aligned}$ | M1  <br> A1  <br> M1  <br> A1  <br> M1  <br> F1  <br>   <br>   <br> A1 cao  <br>  7 | Considering PE or PE at start and finish Award M1 if not more than one error <br> Equation involving KE, PE and EE |
| (iv) | From lowest point to level of A, <br> Loss of EE is 28.665 <br> Gain in PE is $2.5 \times 9.8 \times 0.9=22.05$ <br> Since $28.665>22.05$, <br> Ring will rise above level of $A$ | M1 <br> M1 <br> M1 <br> A1 cao <br> 4 | EE at 'start' and at level of A PE at 'start' and at level of A (For M2 it must be the same 'start') Comparing EE and PE (or equivalent, e.g. $\left.\frac{1}{2} m u^{2}+3.185=m g \times 0.5+\frac{1}{2} m v^{2}\right)$ Fully correct derivation |
|  |  |  | $S R$ If 637 is used as modulus, maximum marks are: <br> (i) B 0 M 1 A 0 <br> (ii) B1M1A1E0 <br> (iii) M1A1M1A1M1F1A0 <br> (iv) M1M1M1A0 |


| 4 (a) | $\begin{aligned} & \text { Area is } \int_{0}^{2} x^{3} \mathrm{~d} x=\left[\frac{1}{4} x^{4}\right]_{0}^{2}=4 \\ & \int x y \mathrm{~d} x=\int_{0}^{2} x^{4} \mathrm{~d} x \\ & =\left[\frac{1}{5} x^{5}\right]_{0}^{2}=6.4 \\ & \begin{array}{l} \bar{x}=\frac{6.4}{4}=1.6 \end{array} \\ & \begin{array}{l} \begin{array}{l} \frac{1}{2} y^{2} \mathrm{~d} x \end{array}=\int_{0}^{2} \frac{1}{2} x^{6} \mathrm{~d} x \\ =\left[\frac{1}{14} x^{7}\right]_{0}^{2}=\frac{64}{7} \\ \bar{y}=\frac{\int \frac{1}{2} y^{2} \mathrm{~d} x}{\int y \mathrm{~d} x} \\ =\frac{\frac{64}{7}}{4}=\frac{16}{7} \end{array} \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 8 | Condone omission of $\frac{1}{2}$ <br> Accept 2.3 from correct working |
| :---: | :---: | :---: | :---: | :---: |
| (b)(i) |  | M1 A1 M1 A1 M1 E1 | 6 | $\pi$ may be omitted throughout <br> For $\frac{5}{3}$ <br> For $\frac{9}{4}$ <br> Must be fully correct |
| (ii) | Height of solid is $h=2 \sqrt{3}$ $\begin{aligned} & T h=m g \times 0.35 \\ & F=T=0.101 \mathrm{mg}, \quad R=m g \end{aligned}$ <br> Least coefficient of friction is $\frac{F}{R}=0.101$ | $\begin{array}{\|l} \hline \text { B1 } \\ \text { M1 } \\ \text { F1 } \\ \text { A1 } \end{array}$ |  | Taking moments <br> Must be fully correct (e.g. A0 if $m=\frac{5}{3} \pi$ is used) |

